

Asymptotic normalization coefficients for $\alpha + {}^{12}\text{C}$ synthesis and the S -factor for ${}^{12}\text{C}(\alpha, \gamma){}^{16}\text{O}$ radiative capture

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The ${}^{12}\text{C}(\alpha, \gamma){}^{16}\text{O}$ reaction, determining the survival of carbon in red giants, is of interest for nuclear reaction theory and nuclear astrophysics. A specific feature of the ${}^{16}\text{O}$ nuclear structure is the presence of two subthreshold bound states, (6.92 MeV, 2^+) and (7.12 MeV, 1^-), that dominate the behavior of the low-energy S -factor. The strength of these subthreshold states is determined by their asymptotic normalization coefficients (ANCs), which need to be known with high accuracy. Recently, using a model-independent extrapolation method, Blokhintsev *et al.* [1] determined the ANCs for the α -particle removal taking into account three subthreshold states in ${}^{16}\text{O}$.

The goal of this work is to address four main problems elucidating the impact of the subthreshold ANCs on the low-energy S -factor. Firstly, we analyze the connection between variations of the subthreshold ANCs and the low-energy S -factor, in particular, at the most effective energy of 300 keV. Secondly, we calculate contributions to the $S(300 \text{ keV})$ -factor from the subthreshold 1^- and 2^+ resonances, that are controlled by the subthreshold ANCs. We also evaluate the contribution of the uncertainties of the subthreshold ANCs to the budget of the $S(300 \text{ keV})$ -factor uncertainty. Thirdly, we analyze interference of the subthreshold resonances with higher resonances and with the E1 and E2 direct captures to the ground state. Finally, we investigate a correlated effect of the subthreshold and ground-state ANCs on the low-energy S -factor and, in particular, on the $S(300 \text{ keV})$ -factor. The S -factors are calculated within the framework of the R-matrix method using the AZURE2 code.

Our total S -factor takes into account the E1 and E2 transitions to the ground state of ${}^{16}\text{O}$ of the interfering subthreshold and higher resonances, which also interfere with the corresponding direct captures, and cascade radiative captures to the ground state of ${}^{16}\text{O}$ through four subthreshold states: 0^+ , 2^+ , 3^- , 2^+ and 1^- . Since our ANCs are higher than those used by deBoer *et al.* [2], the present total S -factor at the most effective astrophysical energy of 300 keV is higher, 174 keVb versus 137 keVb of that work. The contribution to the total E1 and E2 S -factors from the corresponding subthreshold resonances at 300 keV are (71–74)% and (102 – 103)%, respectively. The correlation of the uncertainties of the subthreshold ANCs with the E1 and E2 $S(300 \text{ keV})$ -factors is found. The E1 transition of the subthreshold resonance 1^- does not depend on the ground-state ANC but interferes constructively with a broad (9.585 MeV; 1^-) resonance giving (for the present subthreshold ANC) an additional 26% contribution to the total E1 $S(300 \text{ keV})$ -factor. Interference of the E2 transition through the subthreshold resonance with direct capture is almost negligible for small ground-state ANC of 58 fm $^{-1/2}$. However, the interference with direct capture for higher ground-state ANC of 337 fm $^{-1/2}$ is significant and destructive, contributing -27% . The interference between the E2 transition of the SR 2^+ and direct capture is minimal when the ground-state ANC is small, but becomes destructive at higher ground-state ANC, resulting in a contribution of -27% . The low-energy SE2(300 keV)-factor experiences a smaller increase when both subthreshold and the ground-state ANCs rise together due to their anticorrelation, compared to when only the subthreshold ANCs increase.

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- [1] L.D. Blokhintsev, A.S. Kadyrov, A.M. Mukhamedzhanov and D.A. Savin, Eur. Phys. J. A **59**, 162 (2023).
- [2] R.J. DeBoer *et al.*, Rev. Mod. Phys. **89**, 035007 (2017).